

OKLAHOMA STATE UNIVERSITY  
SCHOOL OF ELECTRICAL AND COMPUTER ENGINEERING



**ECEN 3723 Systems I  
Spring 2003**



**Final Exam**

**Choose any four out of five problems.**  
*Please specify which four listed below to be graded:*  
1)\_\_\_\_; 2)\_\_\_\_; 3)\_\_\_\_; 4)\_\_\_\_;

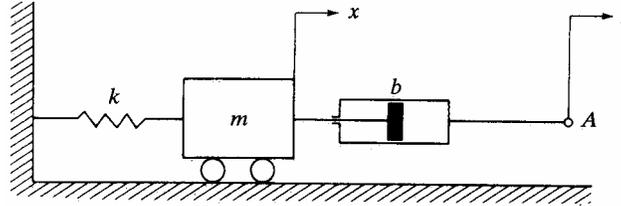
**Name :** \_\_\_\_\_

**Student ID:** \_\_\_\_\_

**E-Mail Address:** \_\_\_\_\_

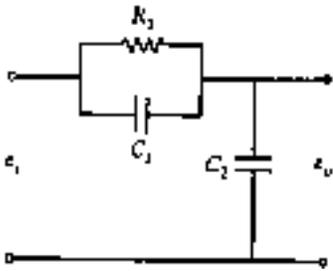
**Problem 1:** (*Time Response*)

The mechanical system shown below is at rest initially. At  $t = 0$ , a unit-step displacement input is applied to point  $A$  (i.e.,  $y(t) = u(t)$ ). Assuming that the system remains linear throughout the response period and is *overdamped*, determine the response  $x(t)$  as well as the values of  $x(0+)$ ,  $\dot{x}(0+)$  and steady state  $x(\infty)$ .

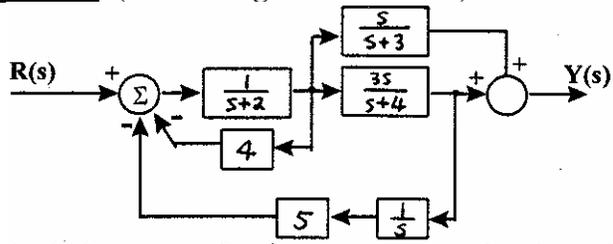


**Problem 2:** (*Frequency Response*)

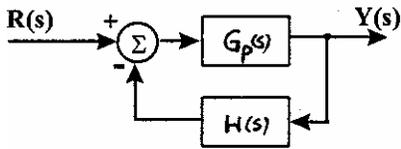
Consider the stable electrical circuits shown below. Assume that the input is sinusoidal,  $e_i(t) = E_i \sin \omega_1 t \cos \omega_2 t$ , determine the steady state output voltage  $e_o(t)$ .



**Problem 3:** (Block Diagram Reduction)



Use block diagram reduction to rearrange the above block diagram into the form shown below and find its transfer function,  $\frac{Y(s)}{R(s)}$ .



**Problem 4:** (*Routh Stability Criteria*)

Find the region of  $K$  in  $G_p(s)$  for which the unity feedback (i.e.,  $H(s) = 1$ ) control system is stable

$$G_p(s) = \frac{K(s^2 + 15s + 55)}{s(s^2 + s + 10)}.$$

**Problem 5:** (*Analogous System*)

Using the force-current analogy, derive an analogous electrical circuit from the mechanical system shown below, where  $p(t)$  is the force input to the system.

